Structural Cointegration Analysis of Private and Public Investment

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Abstract
A structural cointegration approach is used to investigate the relationship between public and private investment, based on datasets which include software in the definitions of investment. Empirical evidence for equipment suggests crowding out. However structures show crowding in, supporting the infrastructure hypothesis.

Key words: structural cointegration approach; public investment

JEL classification: C50; E22; E69

1. Introduction
Studies by Aschauer (1989a, 1989b, 1993) have rekindled interest in the effect of government provision of public investment on the private economy. Short-run Keynesian models which focus on the demand-side effects of government spending conclude that public investment crowds out some though not all private investment spending. However Aschauer, along with Buit (1977), Munnell (1992), and others, also recognizes that public investment may complement private investment by enhancing the productivity of existing resources (the infrastructure hypothesis).

A variety of empirical approaches have been used to estimate the impact of public capital stock on aggregate production technologies or private investment functions [Lynde and Richmond (1992), Erenburg (1993), Evans and Karras (1994), and Demetriades and Mamuneas (2000)]. However two persistent problems have been non-stationarity of variables and the quality of data for public and private investment, at least for national accounts of the United States.

The first purpose of this paper is to use a structural cointegration approach to investigate the relationship between public and private investment. The structural cointegration approach of Pesaran and Pesaran (1997) and Pesaran and Smith (1998) encourages links between the new literature of cointegrating vector autoregressions and the more traditional literature of dynamic structural econometric modeling.
aspects of this approach are the use of theory to identify multiple cointegration vectors and the treatment of stationary or non-stationary exogenous variables. The new literature also suggests the use of model selection criteria, accompanied by diagnostic tests, to specify short-run dynamics, deterministic components, and cointegration rank and includes measuring the speed of convergence to equilibrium with persistence profiles.

A second goal of this paper is to highlight new data series for the U.S. economy which for the first time include spending for computer software in the definitions of public and private investment in equipment [Moulton, Parker, and Seskin (1999)]. The new series are the product of two recent comprehensive revisions which have brought the U.S. accounts into closer conformity with the national accounts of other countries by presenting newly-defined series for government consumption expenditures and government investment. For a discussion of several aspects of the revisions, see Rossiter (2000).

In the results presented below, the structural cointegration approach supports the conclusion that in the long-run public investment in equipment crowds out private investment. However, analysis of investment in structures suggests there is also support for the infrastructure hypothesis, with a convergence to equilibrium which takes several years.

2. Testing the Infrastructure Hypothesis

On the microeconomic level, new theories of investment under uncertainty have been developed based on the intuition of financial options [Hubbard (1994)]. However, on the aggregate level, the infrastructure hypothesis can be most appropriately investigated by a modification of the traditional accelerator cash flow model of private investment.

The distinguishing feature of a traditional accelerator model based on an adjustment cost approach is the assumption that investment depends on changes in output [Eisner and Strotz (1963)]. Empirical specifications commonly include a demand variable such as capacity utilization to capture other business cycles effects. Finally a profit or cash flow variable can be used because profits signal increased future output that increases the optimal path of future capital stock and lowers financing costs.

The traditional accelerator cash flow model can be modified to investigate linkages with public investment by including public investment as an explanatory variable. If higher public investment raises the rate of national capital accumulation, rational private sector agents will alter their investment plans in order to reestablish an optimal level of capital. Thus a modified accelerator cash flow equation may show that public investment crowds out private investment. However Aschauer suggests that there is a second link between public and private investment because public capital raises the return to private capital in private production technology. This second link implies that the stock of public capital crowds in private capital accumulation.
The empirical results below are obtained using fixed investment in equipment or structures, with chained (1996) dollar measures for the nonresidential component of the private sector and for defense, nondefense, and state and local government. Cashflow is corporate profits after taxes, adjusted for inventory valuation and a capital consumption allowance, and output is gross domestic product minus gross housing product. In the empirical work, all variables are measured as logarithms from 1954.1 to 1998.4. The structures and equipment components of public and private investment in chained (1996) dollars are shown in four figures.

**Fig. 1. Private Investment in Equipment**

![Graph showing private investment in equipment over time](image)

**Fig. 2. Private Investment in Structures**

![Graph showing private investment in structures over time](image)
3. Statistical Model

The modified accelerator cash flow model of investment may be appropriately modeled as a structural cointegrating vector autoregression where there are minimal restrictions on short-run dynamics and a long-run cointegration relationship is derived from the accelerator cash flow theory. An appropriate starting point for this approach is an error correction model as in Pesaran and Pesaran (1997) and Pesaran and Smith (1998):
\[ \Delta y_t = a_0 y_t + a_1 x_t - \Pi_y \Delta z_{t-1} + \sum_{i=1}^{p-1} \Gamma_{0i} \Delta z_{t-i} + \Psi_{y} w_t + \epsilon_t, \quad t = 1, 2, \ldots, n, \tag{1} \]

where \( y_t \) is a \((m_y \times 1)\) vector of endogenous \( I(1) \) variables, \( x_t \) is a \((m_x \times 1)\) vector of \( I(1) \) exogenous variables, \( z_t = (y_t', x_t')' \), \( w_t \) is a \((q \times 1)\) vector of exogenous \( I(0) \) variables excluding intercepts and trends, and \( t \) is a time trend. The symbol \( \Delta \) is the difference operator, and all other symbols such as \( a_{0y} \) or \( \Pi_y \) represent coefficients. The model assumes that there is feedback from \( \Delta y \) to \( \Delta x \) but no feedback in levels, so that \( x_t \) is given as

\[ \Delta x_t = a_0 x_t + \sum_{i=1}^{p-1} \Gamma_{xi} \Delta z_{t-i} + \Psi_{x} w_t + \nu_t, \tag{2} \]

and the disturbances \( \epsilon_t \) and \( \nu_t \) are \( iid(0, \Sigma) \) with \( \Sigma \) a symmetric positive-definite matrix, and \( \epsilon_t \) and \( \nu_t \) are distributed independently of \( w_t \). Theory suggests that private and public investment and cashflow can be considered endogenous variables while the utilization rate and change in output are exogenous. If \( y_t \) is cointegrated, the matrix \( \Pi_y \) will have reduced rank with \( r \) cointegration vectors, one or more of which might include private and public investment.

In order to uniquely identify multiple vectors, it would be necessary to impose at least \( r \) restrictions on each of the vectors but if \( r = 1 \), normalization produces exact identification.

If there are linear trends in an unrestricted vector autoregression, cointegration will mean quadratic trends in levels of the variables unless trends are restricted to the cointegrating vectors. If intercepts are restricted to the cointegrating vectors, then \( y_t \) will contain a linear deterministic trend. Thus it is important that equation (1) explicitly models intercepts and trends. If the variables \( y_t \) and \( x_t \) have deterministic trends, the most appropriate action may be to restrict the trend coefficients. Otherwise it would be appropriate to restrict intercepts to the cointegrating vectors.

Lastly, conventional cointegration analysis has used model selection criteria to choose leg length in the error correction model while intercepts and deterministic trends are chosen a priori. Johansen maximum eigenvalue and trace tests are then used to determine the number of cointegration vectors. Mills (1998), Pesaran and Smith (1998), and Phillips (1998) have suggested using a Schwarz or Phillips criterion to select the lag length simultaneously with the number of cointegration vectors and treatment of intercepts and trends. However because many of these tests have low power, the specification of (1) must be confirmed by diagnostic checks for serial correlation. The empirical work presented below uses the Schwarz criterion to specify a statistical model, followed by standard diagnostic tests. All calculations are performed using Microfit 4.0 (Camfit Data Ltd, 1997).
4. Empirical Results

Augmented Dickey-Fuller test statistics were found for each variable, with the number of lags determined by Schwarz criteria. The results presented in Table 1 show that only the utilization rate and the change in output are stationary. Thus in what follows we proceed as if equation (1) contains stationary exogenous variables only.

<table>
<thead>
<tr>
<th>Variable</th>
<th>Number of lags</th>
<th>ADF</th>
</tr>
</thead>
<tbody>
<tr>
<td>Equipment-private</td>
<td>2</td>
<td>-3.277</td>
</tr>
<tr>
<td>Equipment-public</td>
<td>1</td>
<td>-1.447</td>
</tr>
<tr>
<td>Structures-private</td>
<td>1</td>
<td>-1.995</td>
</tr>
<tr>
<td>Structures-public</td>
<td>1</td>
<td>-0.968</td>
</tr>
<tr>
<td>Cashflow</td>
<td>1</td>
<td>-1.948</td>
</tr>
<tr>
<td>Change in output</td>
<td>1</td>
<td>-6.078*</td>
</tr>
<tr>
<td>Utilization rate</td>
<td>1</td>
<td>-4.091*</td>
</tr>
</tbody>
</table>

The Schwarz Bayesian criterion was used to select number of lags. Critical values at the .05 level for the ADF test are -2.880 for private and public structures, change in output and the utilization rate and -3.439 for all other variables.

As a first step in specifying the model, the Schwarz criterion was calculated for lags ranging from 1 to 6 for all possible cointegration vectors for models with either restricted intercepts and no trends or unrestricted intercepts and restricted trends. Using a model selection criterion is advisable given the well-known problems associated with determining the number of cointegration vectors. Specifically, the Johansen trace and maximum eigenvalue tests for cointegration rank perform unreliably in finite samples and often lead to different conclusions. Moreover, the selection of rank is sensitive to the order of the vector-autoregressive component of the model as well as to the treatment of intercepts and trends.

Empirical results for investment in equipment confirm the importance of restricting intercepts or trends when investigating whether a model is cointegrated. In the case of restricted intercepts, the Schwarz criterion consistently suggests a lack of cointegration, with the highest values of the criterion occurring at \( r = 0 \) for lags 1 through 6. (Tabular results for equipment and structures are available upon request.) However in the case of restricted trends, the criterion suggests one cointegration vector at all lags. The maximum value of the criterion occurs when \( r = 1 \) for restricted trends. The maximum value of the criterion occurs
with restricted intercepts, and visual inspection of the data suggests that this is a reasonable choice. Hence a lag length of one is used for structures as well as equipment, with additional tests below to confirm this specification.

Table 2 presents the Johansen maximum eigenvalue and trace tests to determine the number of cointegration vectors for the specifications suggested by the selection criteria. These test statistics strongly support the presence of one cointegration vector for equipment as well as structures. Hence these tests are in agreement with the specification selected using the Schwarz criterion.

<table>
<thead>
<tr>
<th>Equipment</th>
<th>Maximum Eigenvalue Statistic</th>
<th>Trace Statistic</th>
</tr>
</thead>
<tbody>
<tr>
<td>$H_0 : r = 0$</td>
<td>47.27</td>
<td>64.91</td>
</tr>
<tr>
<td>$H_0 : r \leq 1$</td>
<td>10.85</td>
<td>17.64</td>
</tr>
<tr>
<td>$H_0 : r \leq 2$</td>
<td>6.78</td>
<td>6.78</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Structures</th>
<th>Maximum Eigenvalue Statistic</th>
<th>Trace Statistic</th>
</tr>
</thead>
<tbody>
<tr>
<td>$H_0 : r = 0$</td>
<td>42.51</td>
<td>53.64</td>
</tr>
<tr>
<td>$H_0 : r \leq 1$</td>
<td>6.43</td>
<td>11.12</td>
</tr>
<tr>
<td>$H_0 : r \leq 2$</td>
<td>4.69</td>
<td>4.69</td>
</tr>
</tbody>
</table>

For equipment, critical values at the .05 level are 25.42, 19.22, and 12.39 for the maximum eigenvalue test and 42.34, 25.77, and 12.39 for the trace test. For structures, critical values at the .05 level are 25.42, 19.22, and 12.39 for the maximum eigenvalue test and 42.34, 25.77, and 12.39 for the trace test.

<table>
<thead>
<tr>
<th>Equipment</th>
<th>Structures</th>
</tr>
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<tbody>
<tr>
<td>Private Investment</td>
<td>1.000</td>
</tr>
<tr>
<td>Cashflow</td>
<td>0.053 (.060)</td>
</tr>
<tr>
<td>Public Investment</td>
<td>0.276 (.048)</td>
</tr>
<tr>
<td>Trend</td>
<td>-0.018 (.000)</td>
</tr>
</tbody>
</table>

Numbers in parentheses are standard errors.

We normalize on private investment and test the long-run effect of public on private investment. Maximum likelihood estimates of the cointegration coefficients and standard errors are presented in Table 3. In each case, the structural interpretation of the long-run cointegration equation implies that private investment would be the left-hand-side variable. Thus the coefficient on public investment indicates a negative relationship between public investment and private investment in equipment, that is to say, support for the hypothesis that public investment in equipment crowds out private investment. The Chi-square test of the statistical significance of the coefficient is 23.42 ($p = .000$), confirming that public investment should be in-
cluded in the long-run equation for private investment. The coefficient on cashflow is not statistically significant and there is a statistically significant positive trend.

In contrast, the coefficient on public investment in the structures equation is negative, suggesting public investment crowds in private investment. The Chi-square test of the coefficient is 3.12 ($p = .077$). Thus this long-run equation provides weak evidence that public investment in structures crowds in private investment. However the size of the coefficient on public investment is unexpectedly large, as is the negative coefficient on cashflow, so that this equation is not entirely satisfactory. For both structures and equipment, error correction terms were statistically significant in all equations except for public investment, and there was evidence of two-way feedback. Diagnostic statistics for equipment are satisfactory while in the case of structures there is evidence of heteroscedasticity and the adjustment weight in the private investment equation has an unexpected positive sign.

Traditionally the last step in investigating a cointegration model is an impulse response analysis [Lutkepohl and Reimers (1992)]. Koop et al. (1996) have developed a generalized impulse response function which does not require orthogonalization of shocks and is invariant to the ordering of variables. An alternative characterization of the effect of a system-wide shock is a persistence profile, defined as the scaled difference between the conditional variances of the $n$-step and $(n-1)$-step ahead forecasts. A scaled persistence profile will have a value of one on impact but will tend to zero if a relationship is cointegrated (even though the shock will have a permanent effect on the individual variables). In effect, the persistence profile is a test of cointegration which also illustrates the speed with which a relationship returns to equilibrium.

Persistence profiles for equipment and structures (available upon request) confirm the evidence presented above, with a rapid convergence to equilibrium, reasonable for a relationship where crowding out is the result of financial constraints. However the persistence profile for structures suggests that the effect of a system-wide shock persists for many years, supporting the hypothesis that public investment enhances private investment and productivity. However the coefficients of the cointegration vector and incorrect signs of the adjustment coefficients suggest caution in interpreting the structures model overall.

5. Conclusions

This paper uses a structural cointegration approach to test hypotheses of crowding out and crowding in. Empirical results suggest that public investment in equipment crowds out private investment, while public investment in structures has a weak crowding in effect.
References


